## P116B Homework 2

Due 2/1/2019

1. Consider the following logic circuit:

(a) Fill out a truth table for all 16 combinations of the inputs.
(b) Write a logical expression for this circuit, including a logical representation of each individual gate. Do not use the exclusive OR operator $(\oplus)$
(c) Use De Morgan's rule to reduce this to an expression in which any inversions operate only on individual terms.
(d) Design a functionally equivalent circuit using only NAND gates. (Note: It might take quite a few)
2. H\&H 10.13
3. Write a truth table for a "full-subtractor" for calculating the $i^{\text {th }}$ bit of $D=X-Y$, where $B_{i}$ is a request to borrow from bit $i+1$ to bit $i$.


| $B_{i-1}$ | $X_{i}$ | $Y_{i}$ | $D_{i}$ | $B_{i}$ |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 |  |  |
| 0 | 0 | 1 |  |  |
| 0 | 1 | 0 |  |  |
| 0 | 1 | 1 |  |  |
| 1 | 0 | 0 |  |  |
| 1 | 0 | 1 |  |  |
| 1 | 1 | 0 |  |  |
| 1 | 1 | 1 |  |  |

4. Solve the following problems by converting the numbers to binary and solving with twos complemement arithmetic. For the whole numbers, use 8-bit signed integers, and for the numbers with fractions, use fixed-point arithmetic with 8 bits for the fractional part and 16 bits total. Converty back to decimal and verify that your answers are correct.
(a) $65+32$
(b) $19-41$
(c) $12.35+57.6$
(d) $55.2-74.11$
